Understanding the Confusion Matrix

Confusion Matrix

The confusion matrix is a table that summarizes the performance of a classification model by comparing the predicted labels with the actual labels. It is structured as follows:

		true class	
		neg.	pos.
predicted class	neg.	true negative <i>TN</i>	false negative <i>FN</i>
	pos.	false positive FP	true positive <i>TP</i>
		N := TN + FP	P := TP + FN

Definitions and Formulas

Below are the key metrics derived from the confusion matrix:

• Accuracy: Probability that a prediction (positive or negative) is correct:

$$ACC = \frac{TP + TN}{P + N}$$

• Specificity or True Negative Rate: Probability that negative class is correctly predicted:

$$SPC = TNR = \frac{TN}{N}$$

• Recall (Sensitivity) or True Positive Rate: Probability that a positive class is correctly predicted:

$$REC = \frac{TP}{P}$$

• **Precision:** Probability that a positive prediction is correct:

$$PRC = \frac{TP}{TP + FP}$$

• F1 Score: Harmonic mean of precision and recall:

$$F1 = \frac{2TP}{2TP + FP + FN}$$