

# Introduction to Informatics for Students from all Faculties

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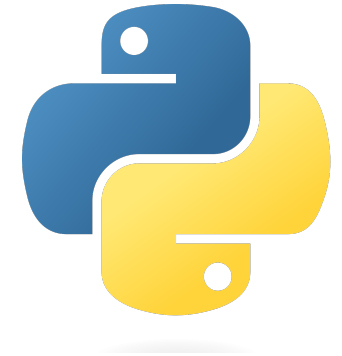
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## Motivation

- ▶ we introduced **high-level programming languages** that are translated to machine code
- ▶ we wrote a first “Hello World” program in C and inspected the machine code generated by the **compiler**
- ▶ we distinguished between **compiled languages** like C/C++ and **interpreted languages** like python
- ▶ we introduced basics of the **python syntax**

### open issues

- ▶ how to write programs that **solve actual problems**?
- ▶ what are **algorithms** and how we can we implement them in high-level languages like python?
- ▶ need to develop **algorithmic thinking**, which is key to understand how a computer (scientist) works



### Notes:

- **Lecture L05: Algorithmic Thinking** 19.11.2024
- **Educational objective:** We introduce algorithms for basic problems like binary search and sorting. We discuss the runtime of algorithms and cover basic data structures.
  - Python Data Structures
  - A Simple Algorithm
  - Binary Search Algorithm
  - Basic Sorting Algorithms
- **Exercise Sheet 4** due 26.11.2024

### Notes:

## Recap: python Syntax

▶ python programs are stored in text files (typically with extension .py)

▶ **one line in text file = one instruction**

### key python statements

- ▶ assignment (=) used to **assign value to a variable**
- ▶ def used to define a **function**
- ▶ import statement used to import functions from modules
- ▶ if and else used to **conditionally execute instructions**
- ▶ for and while used to **repeatedly execute instructions in a loop**

▶ “blocks” of instructions grouped by **indentation level**

▶ python is **whitespace-sensitive**, i.e. placement of newline, space or tab characters changes semantics

▶ python enforces meaningful formatting of code, making programs easy to read for humans

```
import time

def main():
    for i in range(5):
        text = "Hello World!"
        print(text)
        text = 42
        print(text)
    sleep(5)
```

## Integrated Development Environment (IDE)

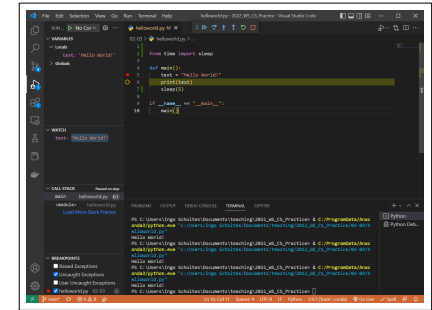
▶ all we need to write python program is **text editor** and **python interpreter** (i.e. executable python.exe)

▶ sufficient for small single-file programs

▶ what about **complex software with hundreds of files and millions of lines in code?**

▶ integrated development environments (IDEs) are specialized tools to **support and simplify development of complex software**

▶ IDEs provide advanced functions to edit and format code, semantically highlight/color keywords, compile and/or execute program, and find errors



Open Source IDE Visual Studio Code

### definition

An **Integrated Development Environment (IDE)** is a software that simplifies the programming of computers. It minimally provides functions to **edit source code files**, compile and/or execute programs, and **find errors at compile- and run-time**.

### Notes:

- Note that the “grammatical structure” of a (programming) language is called “syntax”, which contains the Greek words “syn” (together) and “taxis” (ordering/composition). The syntax of a language defines keywords and determines the ordering of characters that constitutes a valid sentence or (program) in a (programming) language.

### Notes:

## Python Data Structures

- ▶ all programming languages support **basic data types**
  - ▶ integer numbers, i.e. 42, -55, 0
  - ▶ floating point numbers, i.e. 4.52, 1.567e2, 2.0e - 2
  - ▶ character types, i.e. "c", "t"
  - ▶ string types, i.e. "Lecture"
- ▶ python is a **dynamically-typed language**, i.e. we can assign any type to a variable
- ▶ what if we need more **complex structures to store data**?
  - ▶ list of numbers
  - ▶ all sentences of a book
  - ▶ mapping from numbers to text
  - ▶ queue of jobs to be executed in sequence
- ▶ python standard library provides **complex data types** that can hold list, sequences, dictionaries of values

```
import time

def main():
    for i in range(5):
        text = "Hello World!"
        print(text)
        text = 42
        print(text)
    sleep(5)
```

## Python Lists

- ▶ **python lists** can hold **ordered sequence of elements** of any type

### adding / removing elements

- ▶ append allows to **append additional values** at end of list
- ▶ pop can be used to **remove and return element** at a given index (or at the end)
- ▶ remove **deletes first occurrence of a value**
- ▶ we can use zero-based **integer indexing** to read/write elements at specific position
- ▶ **slicing operator [start:end:step]** can be used to return new list with selected elements
- ▶ using append and pop(0) **we can use list as queue**, where elements are returned in **first-in-first-out (FIFO) order**

```
# create list
l = [2, 42, 120, 18, 420]

# adding/removing elements
l.append('hello')
l.remove(120)
print(l.pop())
print(l.pop(0))

# index-based access
l[1] = 43

# elements up to index 2
# (excluding 2)
print(l[:2])

# elements starting from index 1
# (including 1)
print(l[1:])

# initialize list with 42 zero entries
l = [0]*42
```

Notes:

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## Python Tuples

- ▶ by appending, assigning or removing elements, **python lists can dynamically change their size** and **elements can change** during lifetime of list
- ▶ requires complex implementation that makes some operations relatively slow
- ▶ for **fixed-size ordered sequences that cannot change**, we can use python tuples
- ▶ **indexing and slicing** works the same as for lists
- ▶ elements cannot change and size of tuple cannot grow or shrink
- ▶ we can use + operator to **concatenate two tuples**, returning a new tuple

```
# create tuple
t = (2, 42, 120, 189, 420)

# index-based access
print(t[1])

# slicing
print(t[:2])
print(t[1:])

# NOT VALID
t[1] = 43

# returns new tuple with additional
# elements
t2 = t + (4,5,6)
print(t2)
```

## Python Sets

- ▶ lists and tuples are **ordered sequences**
- ▶ checking whether an **element is in a list/tuple** requires to **test all elements** → naive linear search
- ▶ for **unordered collection of objects without duplicates** we can use python set
- ▶ useful to **eliminate duplicate elements** and **quickly test for membership**
- ▶ **python sets** are unordered and thus **do not support indexing or slicing**

```
# create set
s = {2, 'hello', 120, 42, 189, 420}
print(s)

# check membership
print('hello' in s)

# add element
s.add(32)

# remove element
s.remove('hello')

# NOT VALID
s[1]
s[:4]
```

Notes:

Notes:

## Python Dictionaries

- ▶ we often need an **associative mapping** that maps **unique keys** to values
  - ▶ string/number as unique identifier (key)
  - ▶ arbitrary data of record (value)
- ▶ useful to **quickly find data** that are stored under a given key
- ▶ we can read/write entries using **index syntax** similar to lists
- ▶ **but:** index does not need to be an integer
- ▶ **reverse lookup** (i.e. find key(s) for a given value) not supported

```
# create dictionary
d = { 'hello': 'Hallo',
      'world': 'Welt',
      'teacher': ['Ingo', 'Scholtes']
}

# check membership of key
print('hello' in d)

# access value of given key
print(d['hello'], d['teacher'])

# assign value to (new) key
d['audience'] = 'Studierende'
```

## Practice Session

- ▶ we show how to install the Open Source **python distribution Anaconda**
- ▶ we use the **integrated development environment (IDE)** Visual Studio Code to write and execute a simple python program
- ▶ we use VS Code to **rename variables and refactor code**
- ▶ we use the **debugger of Visual Studio Code** for a step-wise execution of python statements
- ▶ we demonstrate lists, tuples, sets, and dictionaries in python

```
import time
```

```
def main():
    text = "Hello World!"
    print(text)
    text = 42
    print(text)
    sleep(5)
```

### practice session

see directory 05-01 in **gitlab** repository at

→ [https://gitlab2.informatik.uni-wuerzburg.de/ml4nets\\_notebooks/2024\\_wise\\_infhaf\\_notebooks](https://gitlab2.informatik.uni-wuerzburg.de/ml4nets_notebooks/2024_wise_infhaf_notebooks)

Notes:

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# What is an algorithm?

**definition** → L01 - Motivation

An **algorithm** is a sequence of precisely defined (mathematical) instructions that must be executed to solve a given problem.

- ▶ algorithm takes a (possibly empty) **input** and produces – after a **finite number of steps** – a desired **output**
- ▶ expressing an algorithm in terms of a **programming language** allows us to **implement** it on a computer

**Example: pencil-and-paper algorithm to add two numbers**

- step 1 start at right-most position
- step 2 add digits at current position
- step 3 write last digit of sum below current position
- step 4 for sums  $\geq 10$  additionally **carry over 1** to position on the left
- step 5 move one position to left and go to step 2

$$\begin{array}{r} 1 \quad 2 \quad 5 \quad 7 \\ 2_1 \quad 9 \quad 3 \quad 2 \\ \hline 4 \quad 1 \quad 8 \quad 9 \end{array}$$

**Notes:**

# Group Exercise 05-01

- ▶ Assume that we want to implement the **pen-and-pencil algorithm to add two decimal numbers with an arbitrary number of digits**. Specify a reasonable input and output of this algorithm.

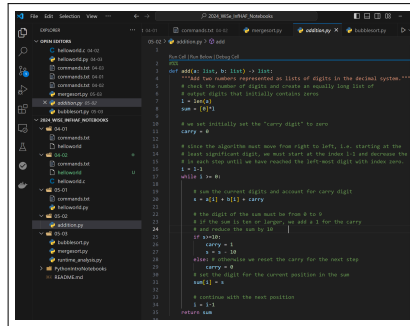
- ▶ Develop a python function `add` that implements the pen-and-pencil algorithm, using control structures like `while`, `for`, `if` as well as a python list

**Notes:**

- In lecture L02 we have seen how we can use digital logics to implement the addition of two binary numbers in terms of hardware. Thanks to the fact that this operation is implemented in the ALU of the CPU, we can directly add two 32 or 64 bit numbers by a single machine instruction (e.g. `ADD`). This implies that we can use the `ADD` operator `+` in high-level languages like python, which is directly mapped to this machine instruction.
- As an exercise, we pretend that there was no such operation that allows to add numbers with more than one digit. Let us implement the **pen-and-pencil algorithm to add decimal numbers** in python.
- Note that such an algorithm can still be useful if we want to add two numbers that cannot be represented by 64 bits or less, which may not be supported by the ALU of a common CPUs.

## Practice Session

- ▶ we use lists to **implement the algorithm** developed in the previous group exercise in python
- ▶ we **test our algorithm** with different inputs



```
def add(a: list[int], b: list[int]) -> list[int]:
    """Add two numbers represented as lists of digits in the decimal system.
    a and b are lists of digits and must be non-empty, non-null and
    contain digits that initially contain zero.
    a: [1, 2, 3, 4]
    b: [5, 6, 7]
    sum: [6, 9, 1]"""
    # we will initially set the 'carry digit' to zero
    carry = 0
    # since the algorithm must move from right to left, i.e. starting at the
    # least significant digit, we must start at the end of a and traverse the
    # list from right to left until we have reached the left-most digit with index zero
    i = len(a) - 1
    j = len(b) - 1
    # use the current digits and account for carry digit
    k = a[i] + b[j] + carry
    # the digit of the sum must be from 0 to 9
    # if the sum is ten or larger, we add a 1 for the carry
    # and reduce the sum by 10
    if k >= 10:
        carry = 1
        k = k - 10
    else:
        carry = 0
    # store the digit for the current position in the sum
    sum.append(k)
    # continue with the next position
    i -= 1
    j -= 1
    # continue until we reach the end of the list
    while i >= 0 or j >= 0:
        k = a[i] + b[j] + carry
        if k >= 10:
            carry = 1
            k = k - 10
        else:
            carry = 0
        sum.append(k)
        i -= 1
        j -= 1
    # if there is still a carry, we add it to the sum
    if carry:
        sum.append(carry)
    # reverse the sum
    sum.reverse()
    return sum
```

### practice session

see directory 05-02 in gitlab repository at

→ [https://gitlab2.informatik.uni-wuerzburg.de/ml4nets\\_notebooks/2024\\_wise\\_infhaf\\_notebooks](https://gitlab2.informatik.uni-wuerzburg.de/ml4nets_notebooks/2024_wise_infhaf_notebooks)

## Search problems

- ▶ we are frequently confronted with **standard problems** that can be solved by well-understood **standard algorithms**
- ▶ exemplary standard problem: search for an object

### search problems

Search problems are a class of problems that seek to quickly **find a given object** within a certain **data structure**.

- ▶ examples
  - ▶ problem 1: search name "Turing" in arbitrary list of 10,000 names
  - ▶ problem 2: search name "Turing" in a phonebook
- ▶ optimal solution to the search problem depends on **prior knowledge on the data structure**



image credit: DALL-E generated image, prompt "needle in a haystack"

Notes:

Notes:

## Searching in sorted data

- ▶ we can **sort a list of objects** whenever for pair of objects  $a$  and  $b$  we can determine whether  $a \geq b$
- ▶ we assume that we search object  $x$  in a **list sorted in ascending order**, i.e. list  $l$  where for index  $i$  we have

$$l[i + 1] \geq l[i]$$

- ▶ **naive algorithm** checks  $x == l[i]$  for index  $i = 0, 1, \dots$

### binary search algorithm

- ▶ test if  $x$  is larger/smaller/equal than middle element  $c$
- ▶ if  $x == c$  return object
- ▶ if  $x > c$  repeat search in elements **right of  $c$**
- ▶ if  $x < c$  repeat search in elements **left of  $c$**

- ▶ binary search is example for **divide-and-conquer algorithm**

- ▶ both algorithms give correct result, but **which one is "better"?**

searching for  $x = 17$

sorted list

|   |   |   |    |    |    |    |
|---|---|---|----|----|----|----|
| 2 | 3 | 5 | 11 | 17 | 23 | 47 |
|---|---|---|----|----|----|----|

step one

|   |   |   |    |    |    |    |
|---|---|---|----|----|----|----|
| 2 | 3 | 5 | 11 | 17 | 23 | 47 |
| - | - | - | -  | 17 | 23 | 47 |

step two

|   |   |   |   |    |    |    |
|---|---|---|---|----|----|----|
| - | - | - | - | 17 | 23 | 47 |
| - | - | - | - | 17 | -  | -  |

step three

|   |   |   |   |    |   |   |
|---|---|---|---|----|---|---|
| - | - | - | - | 17 | - | - |
|---|---|---|---|----|---|---|

found  $x = 17!$

## Complexity of binary search

1/2

we can evaluate algorithms in terms of **computational complexity**, i.e. we count how many steps they **maximally require** to produce the correct output for a given input?

example 1: how many steps do we need in list  $l$  with **32 objects**

### naive (linear) search algorithm

| step | tested element |
|------|----------------|
| 1    | 0              |
| 2    | 1              |
| 3    | 2              |
| ...  | ...            |
| 32   | 31             |

requires **32 steps for 32 objects**

### binary search algorithm

| step | tested element                                     |
|------|--|
| 1    | 16   |
| 2    | 8 or 24  |
| 3    | 4, 12, 20, or 28                                   |
| 4    | 2, 6, 10, 14, 18, 22, 26, or 30                    |
| 5    | 0, 1, 3, 5, 7, 8, 9, 11, 13, 15, 16, 17, ... or 31 |

requires **5 steps for 32 objects**

Notes:

Notes:



## Complexity of binary search

2/2

we can evaluate algorithms in terms of **computational complexity**, i.e. we count how many steps they **maximally require** to produce the correct output for a given input?

example 2: how many steps do we need in list  $l$  with **64 objects**

### naive (linear) search algorithm

| step | tested element |
|------|----------------|
| 1    | 0              |
| 2    | 1              |
| 3    | 2              |
| 4    | 3              |
| ...  | ...            |
| 63   | 64             |

requires **64 steps for 64 objects**

### binary search algorithm

| step | tested element                         |
|------|--|
| 1    | 32                                     |
| 2    | 16 or 48                               |
| 3    | 8, 24, 40, or 56                       |
| 4    | 4, 12, 20, 28, ... or 60               |
| 5    | 2, 6, 10, 14, 18, 22, ... or 62        |
| 6    | 0, 1, 3, 5, 7, 9, 11, 13, 15 ... or 63 |

requires **6 steps for 64 objects**

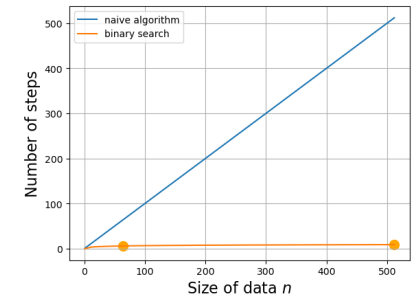
## Linear vs. logarithmic complexity

- ▶ naive search algorithm requires one step for each entry in the input list, i.e. runtime is **proportional to the input size**
- ▶ we say an algorithm has **linear complexity** if for input with size  $n$  it requires at most

$$c + x \cdot n$$

steps for some numbers  $c$  and  $x$

- ▶ thanks to sorted input, **binary search algorithm** requires **less than linear** number of steps
- ▶ how does number of steps grow as we increase input size  $n$ ?

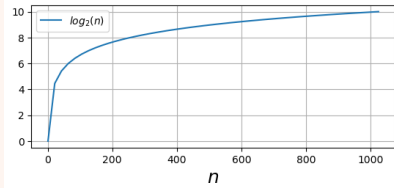


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# Logarithms

## Logarithm



For a number  $n$ , the logarithm  $\log_b(n)$  with base  $b$  of  $n$  is the number  $x$  such that  $b^x = n$ .

logarithms base  $b = 2$

| $n$        | binary number | $\log_2(n)$ |
|------------|---------------|-------------|
| $2^0 = 1$  | 1             | 0           |
| $2^1 = 2$  | 10            | 1           |
| $2^2 = 4$  | 100           | 2           |
| $2^3 = 8$  | 1000          | 3           |
| $2^4 = 16$ | 10000         | 4           |

logarithms base  $b = 10$

| $n$            | $\log_{10}(n)$ |
|----------------|----------------|
| $10^0 = 1$     | 0              |
| $10^1 = 10$    | 1              |
| $10^2 = 100$   | 2              |
| $10^3 = 1000$  | 3              |
| $10^4 = 10000$ | 4              |

# Complexity of search algorithms

we can evaluate algorithms in terms of **computational complexity**, i.e. we count how many steps they **maximally require** to produce the correct output for a given **input of size  $n$** ?

how many steps do we need in list  $l$  with  $n = 64$  objects

## naive (linear) search algorithm

| step | tested element |
|------|----------------|
| 1    | 0              |
| 2    | 1              |
| 3    | 2              |
| 4    | 3              |
| ...  | ...            |
| 64   | 63             |

requires  $n$  steps for  $n$  objects

## binary search algorithm

| step | tested element                         |
|------|--|
| 1    | 32                                     |
| 2    | 16 or 48                               |
| 3    | 8, 24, 40, or 56                       |
| 4    | 4, 12, 20, 28, ... or 60               |
| 5    | 2, 6, 10, 14, 18, 22, ... or 62        |
| 6    | 0, 1, 3, 5, 7, 9, 11, 13, 15 ... or 63 |

requires  $\log_2 n$  steps for  $n$  objects

## Notes:

- It is easy to see that  $\log_b(n)$  increases proportionally with the number of digits of  $n$  in a  $b$ -nary numeral system

## Notes:

## Sorting problem

- ▶ for binary search, we assumed that the list of objects is **sorted**
- ▶ to sort objects we must be able to **compare them**, i.e. for each pair  $a, b$  we must be able to determine  $a \geq b$
- ▶ how can we compare pairs of
  - ▶ numbers,
  - ▶ words,
  - ▶ books,
  - ▶ emojis?

### sorting problem

The **sorting problem** refers to the problem of sorting a list of **pairwise comparable objects** in ascending or descending order.

- ▶ in the following, we consider the sorting problem for a list of **integer numbers**

input:

|   |   |    |    |   |    |
|---|---|----|----|---|----|
| 7 | 2 | 47 | 23 | 5 | 11 |
|---|---|----|----|---|----|

desired output:

|   |   |   |    |    |    |
|---|---|---|----|----|----|
| 2 | 5 | 7 | 11 | 23 | 47 |
|---|---|---|----|----|----|

## BubbleSort algorithm

- ▶ simple idea: repeatedly **compare pairs** of numbers and **swap them** if they are in the wrong order
- ▶ with each swap ...
  - ▶ larger numbers progressively move to right
  - ▶ smaller numbers progressively move to left
- ▶ in each pass of the algorithm, we must compare **all subsequent pairs** of numbers in the list
- ▶ if we have zero swaps during a pass, we know that the list is sorted!
- ▶ in the example, we needed
  - ▶  $4 \cdot 5 = 20$  comparisons
  - ▶  $4 + 2 + 1 = 7$  swaps
- ▶ how many comparisons do we need in **best/worst case**?

third pass

|   |   |   |    |    |    |
|---|---|---|----|----|----|
| 2 | 7 | 5 | 11 | 23 | 47 |
| 2 | 7 | 5 | 11 | 23 | 47 |
| 2 | 7 | 5 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |
| 2 | 5 | 7 | 11 | 23 | 47 |

5 comparisons, 1 swap

Notes:

Notes:

## Worst-case complexity of BubbleSort

### worst-case runtime

For an input **list sorted in reverse order** BubbleSort algorithm requires  $n$  passes with  $n - 1$  comparisons each.

|    |    |    |   |   |   |
|----|----|----|---|---|---|
| 47 | 23 | 11 | 7 | 5 | 2 |
|----|----|----|---|---|---|

$$n = 6$$

$$n \cdot (n - 1) = 6 \cdot 5 = 30 \text{ comparisons}$$

### best-case runtime

For an input **list that is already sorted** BubbleSort algorithm requires a single pass with  $n - 1$  comparisons.

|   |   |   |    |    |    |
|---|---|---|----|----|----|
| 2 | 7 | 5 | 11 | 23 | 47 |
|---|---|---|----|----|----|

$$n = 6$$

$$n - 1 = 5 \text{ comparisons}$$

## Linear vs. polynomial complexity

- ▶ for input list with  $n$  elements, BubbleSort has **worst-case runtime** of

$$n \cdot (n - 1) = n^2 - n$$

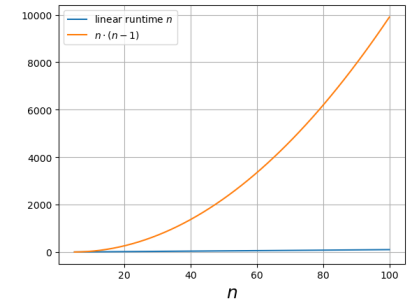
i.e. number of required steps grows as **second power (i.e. square) of input size  $n$**

- ▶ we call expressions of the form

$$a_k \cdot n^k + a_{k-1} \cdot n^{k-1} + \dots + a_0 \cdot n^0$$

**polynomial**

- ▶ for polynomials with power larger than one, runtime **grows over-proportionally** with input size



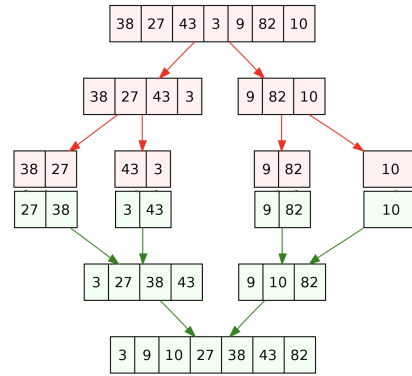
linear vs. polynomial growth of complexity

Notes:

Notes:

## MergeSort

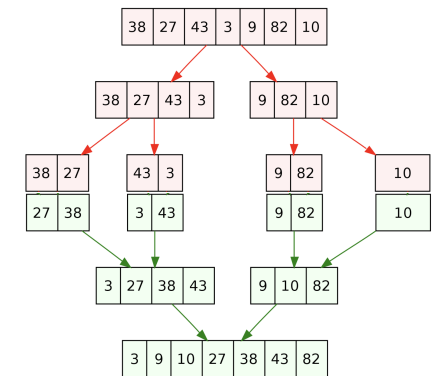
- ▶ can we **sort a list faster** than BubbleSort?
- ▶ assume that we have **two already sorted lists**  $l_1$  and  $l_2$
- ▶ in  $n = n_1 + n_2$  steps we can **merge**  $l_1$  and  $l_2$  into a new sorted list  $l$
- ▶ we can apply **divide-and-conquer idea** behind binary search to sorting
- ▶ phase 1: repeatedly **split** input until we are left with lists with one element (which are already sorted)
- ▶ phase 2: repeatedly **merge** increasingly large (sorted) lists until full list is sorted



## Complexity of MergeSort

- ▶ assume that for a **list with  $n$  elements** MergeSort takes  $T(n)$  steps
- ▶ each split/merge then requires
 
$$2 \cdot T\left(\frac{n}{2}\right) + n$$
- ▶ starting with  $T(1) = 0$  we have
  - ▶  $T(2) = 2 \cdot T(1) + 2 = 2$
  - ▶  $T(4) = 2 \cdot T(2) + 4 = 2 \cdot 2 + 4 = 8$
  - ▶  $T(8) = 2 \cdot T(4) + 8 = 2 \cdot 8 + 8 = 24$
  - ▶  $T(16) = 2 \cdot T(8) + 16 = 2 \cdot 24 + 16 = 64$
  - ▶ ...
- ▶ we can calculate runtime of MergeSort as

$$T(n) \approx n \cdot \log_2(n)$$

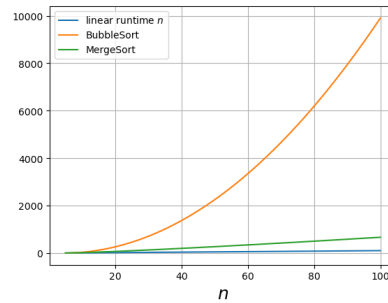


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## Complexity of sorting?

- ▶ with BubbleSort we can sort  $n$  numbers in  $n - 1$  steps in best case and  $n \cdot (n - 1)$  in worst case
- ▶ MergeSort improves worst-case complexity of BubbleSort from  $n^2$  to  $n \log_2(n)$
- ▶ **on average** MergeSort requires  $n \log_2(n)$  steps
- ▶ to sort  $n$  objects based on **pairwise comparisons**, there is **no algorithm exist that requires less than  $n \log_2(n)$  steps on average**
- ▶ **but:** there are specialized algorithms to **sort  $n$  integer numbers in a fixed range** with linear runtime → self-study

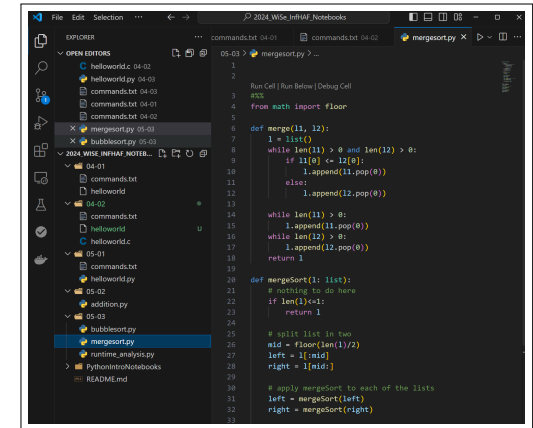


worst-case complexity of MergeSort vs. BubbleSort

questions

## Practice Session

- ▶ we implement BubbleSort in python
- ▶ we implement the divide-and-conquer method MergeSort
- ▶ we study the **runtime of both algorithms** in increasingly large input lists



practice session

see directory 05-03 in [gitlab repository](https://gitlab2.informatik.uni-wuerzburg.de/m4nets_notebooks/2024_wise_infhaf_notebooks) at

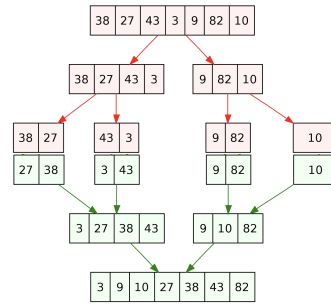
→ [https://gitlab2.informatik.uni-wuerzburg.de/m4nets\\_notebooks/2024\\_wise\\_infhaf\\_notebooks](https://gitlab2.informatik.uni-wuerzburg.de/m4nets_notebooks/2024_wise_infhaf_notebooks)

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## In summary

- ▶ we covered basic **python data structures** like sets, tuples, lists, and dictionaries
- ▶ we introduced **basic algorithms for standard computational problems** like searching and sorting
- ▶ we evaluated the **computational complexity** of sort and search algorithms
- ▶ we highlighted the difference between **logarithmic, linear, and polynomial runtime**



## Self-study questions

1. Explain the differences between a set, a tuple, a dictionary and a list in python.
2. Give a formulation of the Pen-And-Pencil algorithm to add two numbers in python and explain it in your own words.
3. Extend the Pen-And-Pencil algorithm from the group exercise such that it can add numbers given as sequences of digits in an arbitrary  $k$ -nary numeral system.
4. Give a formulation of the Binary Search algorithm in python and explain it in your own words.
5. Could we generalize the Binary Search algorithm such that in each step we split the list into three equally large parts, which would lead to a runtime  $\log_3(n)$ ?
6. Give a formulation of the BubbleSort algorithm in python and explain it in your own words.
7. Give an example for an input for which the BubbleSort algorithm performs the maximum/minimum number of comparisons.
8. Count the number of swaps in an input list with  $n$  elements, where BubbleSort performs the maximum number of comparisons.
9. Give a formulation of the MergeSort algorithm in python and explain it in your own words.
10. Investigate the BucketSort algorithm for integers in a fixed range and explain why it takes less than  $n \log_2 n$  steps on average.

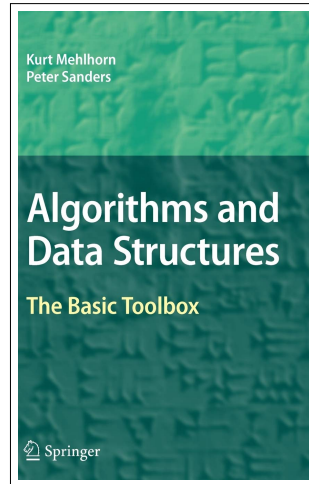
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# Literature

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## Notes: