

$$\mathbb{Z}_2 \times \mathbb{Z}_2 = \{(\bar{0}, \bar{0}), (\bar{1}, \bar{0}), (\bar{0}, \bar{1}), (\bar{1}, \bar{1})\}$$

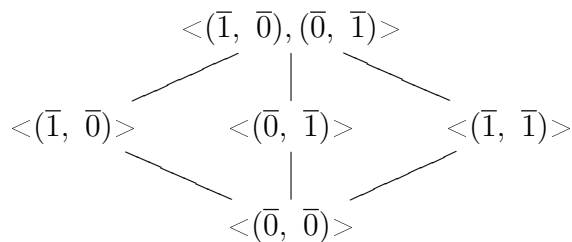
$$\text{ord}(\bar{0}, \bar{0}) = 1$$

$$\text{ord}(\bar{1}, \bar{0}) = 2 \quad \left((\bar{1}, \bar{0}) + (\bar{1}, \bar{0}) = (\bar{2}, \bar{0}) = (\bar{0}, \bar{0}) \right)$$

$$\text{ord}(\bar{0}, \bar{1}) = 2 \quad \left((\bar{0}, \bar{1}) + (\bar{0}, \bar{1}) = (\bar{0}, \bar{2}) = (\bar{0}, \bar{0}) \right)$$

$$\text{ord}(\bar{1}, \bar{1}) = 2 \quad \left((\bar{1}, \bar{1}) + (\bar{1}, \bar{1}) = (\bar{2}, \bar{2}) = (\bar{0}, \bar{0}) \right)$$

Untergruppenstruktur von $\mathbb{Z}_2 \times \mathbb{Z}_2$



Die einzigen Untergruppen in \mathbb{Z}_2 sind $\langle \bar{0} \rangle$ und $\langle \bar{1} \rangle = \mathbb{Z}_2$.

$$\langle (\bar{0}, \bar{0}) \rangle = \langle \bar{0} \rangle \times \langle \bar{0} \rangle$$

$$\langle (\bar{1}, \bar{0}) \rangle = \langle \bar{1} \rangle \times \langle \bar{0} \rangle$$

$$\langle (\bar{0}, \bar{1}) \rangle = \langle \bar{0} \rangle \times \langle \bar{1} \rangle$$

$$\mathbb{Z}_2 \times \mathbb{Z}_2 = \langle \bar{1} \rangle \times \langle \bar{1} \rangle$$

Die Untergruppe $\langle (\bar{1}, \bar{1}) \rangle$ ist folglich nicht darstellbar als direktes Produkt von Untergruppen.