6. Language Modeling for Retrieval

Prof. Dr. Goran Glavaš

Center for AI and Data Science (CAIDAS) Fakultät für Mathematik und Informatik Universität Würzburg



CreativeCommons Attribution-NonCommercial-ShareAlike 4.0 International

After this lecture, you'll...

Know what a language model is

2

- Understand differences between different language models (unigram, bigram)
- Understand how to use language modeling for information retrieval
- Learn about different smoothing schemes for LM for IR
- Be able to compare LM for IR with vector space model and classic probabilistic models

Outline

- Recap of Lecture #5
- Language Models
 - Unigram LM
 - Bigram LM
- Query likelihood model for ranking
- Smoothing schemes
- Projects
 - Topics explained
 - Organization

Recap of the previous lecture

- 4
- Probabilistic retrieval
 - **Q:** Why probability theory in IR, and why probabilistic ranking?
 - **Q:** What are the uncertainties of the IR process that we model probabilistically?
- Probability ranking principle
 - **Q:** What does Robertson's probabilistic ranking principle say?
 - **Q:** How do we formalize the probability ranking principle?
- Probabilistic ranking
 - **Q:** What is the ranking task formulation in the probabilistic setting?
 - Q: Starting from (log-)odds of relevance, how do we derive the general probabilistic ranking score?
- Binary independence model and extensions
 - **Q:** What assumptions does binary independence model introduce?
 - **Q:** What does the ranking function look like under these assumptions?
 - **Q:** Derive the BIM ranking function with and without relevance judgements
 - Q: How do Two Poisson, BM11, and BM25 extend BIM? What assumptions do they introduce?

Recap of the previous lecture

The ranking score at the core of all probabilistic models:

$$\log\left(\frac{P(D|Q,r)}{P(D|Q,\bar{r})}\right)$$

Ranking function of Binary Independence Model

Without (left) and with (right) relevance judgements

$$\begin{aligned} \operatorname{rel}(D,Q) &= \sum_{t \in Q} \log\left(\frac{P(D_t|Q,r)}{P(D_t|Q,\bar{r})}\right) & \operatorname{rel}(D,Q) = \sum_{t \in Q} \log\left(\frac{P(D_t|Q,r)}{P(D_t|Q,\bar{r})}\right) \\ &= \sum_{t \in Q} \log\left(\frac{0.5}{\frac{N_t}{N}}\right) & = \sum_{t \in Q} \log\left(\frac{\frac{r_t + 0.5}{R+1}}{N-R+1}\right) \\ &= \sum_{t \in Q} \log\left(0.5 \cdot \frac{N}{N_t}\right) & = \sum_{t \in Q} \log\left(\frac{(r_t + 0.5) \cdot (N-R+1)}{(R+1) \cdot (N_t - r_t + 0.5)}\right) \end{aligned}$$

Binary independence model – example #1

- 6
- Example for BIM (without relevance judgements)
- Document collection consists of the following documents:
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- The query is: "Sam stabbed orc"

	d_1			d_2		d_3
t	Sam	stabbed	orcs	Sam	orc	Sam
$P(D_t q,r)$	0.5	0.5	0.5	0.5	0.5	0.5
$P(D_t q,\bar{r})$	3/3	1/3	2/3	3/3	2/3	3/3
w_t	0.5	1.5	0.75	0.5	0.75	0.5
$\sum w_t$	2.75			1.25		0.5

Note: computations in this example are done without taking the logarithm

Binary independence model – example #2

- 7
- Example for BIM (with available relevance judgements)
- Document collection contains N = 30 documents, including:
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- The query is: "Sam stabbed orc"
- User has indicated R = 6 relevant documents for this query
- Query terms: t₁ = "Sam", t₂ = "stab", t₃ = "orc"
- Document frequencies of query terms in relevant documents and overall collection are given as follows:
 - r_{t1} = 3, N_{t1} = 15
 - r_{t2} = 4, N_{t2} = 16
 - r_{t3} = 2, N_{t3} = 14

Binary independence model – example #2

8

Example for BIM (with available relevance judgements)

		d_1		d	2	d_3
t	Sam	stabbed	orcs	Sam	orc	Sam
$P(D Q,r) = \frac{r_t + 0.5}{R+1}$	0.5	0.64	0.36	0.5	0.36	0.5
$P(D Q,r) = \frac{r_t + 0.5}{R+1}$ $P(D Q,\bar{r}) = \frac{N_t - r_t + 0.5}{N - R + 1}$	0.5	0.5	0.5	0.5	0.5	0.5
w_t	1	1.28	0.72	1	0.72	1
$\sum_t w_t$		3		1.'	72	1

Note: computations in this example are done without taking the logarithm

Outline

- Recap of Lecture #5
- Language Models
 - Unigram LM
 - Bigram LM
- Query likelihood model for ranking
- Smoothing schemes

Language Modeling (for Information Retrieval)

- 10
- Language models are probabilistic models that capture the probabilities of sequences of words in a language
 - Unigram model: how likely is the word "frodo" to appear (in a language)?
 - P("frodo") = ?
 - Bigram model: given that current word is "frodo", what is the probability of next word being "baggins"?
 - P("baggins" | "frodo") = ?
 - Trigram model: given the current sequence "frodo baggins", what is the probability of next word being "shire"?
 - P(",shire" | ",frodo baggins") = ?
- Q: How do we estimate probabilities of words and sequences in a language?
 - I.e., What do we use as a representation of the language?

Language Modeling (for Information Retrieval)

- 11
- We use the instantiations of the language to estimate the probabilities of words and sequences
 - I.e., large corpora the larger the corpora, it is the better approximation of the true word distributions in language
- In other applications we build language models largest corpora we can compile
- In information retrieval, we build language models
 - 1. From individual documents
 - 2. From the whole document collections

Language Modeling (for Information Retrieval)

- 12
- Language models for IR are also probabilistic models
- Language models for IR model the query generation process
- Given a documet d and a query q, what is the probability of <u>query being sampled</u> from the <u>language model of the document</u>
- In other words, we want to estimate P(Q = q | D = d)
 - Q: Compare this with the probability we estimated in classic probabilistic retrieval
 P(R = 1 | Q = q, D = d)
- The probability of a document generating a query is directly the function according to which we rank the documents

I.e., We rank the documents in decreasing order of P(Q = q | D = d)

Key question: how do we estimate P(Q = q | D = d)?

Language Bowl Metaphor

- Assume we have a document in with following occurrences of terms:
 - "frodo" (5x), "baggins" (3x), "sam" (3x), "shire" (2x), "gandalf" (2x), "orc" (1x)
- Let's represent each term with balls of one color:
 - "frodo" -> 5 blue balls, "baggins" -> 3 red balls, "sam" -> 3 yellow balls
 - shire" -> 2 green balls, "gandalf" -> 2 orange balls, "orc" -> 1 purple ball
- We put all balls into one bowl and randomly take them out one by one
- Q: What is the probability of drawing a yellow ball?

P()) = P(,,sam'') = 3 / (5 + 3 + 3 + 2 + 2 + 1) = 3 / 16

- **Q:** What is the probability of drawing first orange then blue ball?
 - Replacement: P(,) = P(,gandalf", ,frodo") = P(,gandalf") * P(,frodo") = 2/16 * 5/16
 - No replacement: P(,) = P(,gandalf", ,frodo") = P(,gandalf") * P(,frodo" | ,gandalf")
 = 2/16 * 5/15

Language Model – Generative Story

- Language model can be observed as a statistical model for generating data
- Example (toy language, consisting of four words):
 - P("frodo") = 0.3, P("sam") = 0.25, P("gandalf") = 0.35, P("shire") = 0.1
 - P("sam" | "frodo") = 0.4, P("gandalf" | "frodo") = 0.4, P("shire" | "frodo") = 0.2
- Generative process:
 - 1. Randomly draw the first word (e.g., from a uniform distribution)

frodo sam	gandalf	shire
-----------	---------	-------

2. Draw the second word from conditional distribution of the first word (e.g., "frodo")

sam | frodo gandalf | frodo shire | frodo

• **Q:** What is the probability of the sequence *"frodo shire"*?

Types of Language Models

We want to estimate the probability of the sequence:

 $\mathsf{P}(\bigcirc \bigcirc \bigcirc \bigcirc) = \mathsf{P}(\bigcirc) * \mathsf{P}(\bigcirc | \bigcirc) * \mathsf{P}(\bigcirc | \bigcirc \bigcirc) * \mathsf{P}(\bigcirc | \bigcirc \bigcirc \bigcirc) * \mathsf{P}(\bigcirc | \bigcirc \bigcirc \bigcirc)$

- Unigram language model
 - Word independence = probability of the word does not depend on previous words
 - We ignore conditioning

 $\mathsf{P}(\bigcirc \bigcirc \bigcirc \bigcirc) = \mathsf{P}(\bigcirc) * \mathsf{P}(\bigcirc) * \mathsf{P}(\bigcirc) * \mathsf{P}(\bigcirc)$

Bigram language model

- The probability of word appearing depends only on the immediately preceding word
- Conditioning only one one word before

 $P(\bigcirc \bigcirc \bigcirc \bigcirc) = P(\bigcirc) * P(\bigcirc \bigcirc) * P(\bigcirc \bigcirc) * P(\bigcirc \bigcirc)$

• Q: N-gram models for $N \ge 3$ are rarely used in practice. Why?

Sparseness issue of language models

Language models have a major issue

- The longer the phrase, the harder it is to estimate its true probability in language
- E.g., P(",bilbo" | "frodo ran around house found ring") = ?
- Long phrases have very few appearances even in very large corpora
 - Impossible to compute reliable estimates of their conditional probabilities
 - This is why language models for $N \ge 3$ are almost never used
- In practice, we use unigram and bigram language models
 - In IR setting, we build language models from invidual documents
 - Even bigram probability hard to estimate
 - In IR, we most often employ the unigram language model

Estimating probabilities

- For the unigram language model we need to estimate
 - P(term) for every term in the text
- For the bigram language model we additionally need to estimate
 - P(term | previous term) for every pair of terms that appear one after another
- Q: How do we estimate these?
 - Unigram language model
 - $P(t_i) = n_i / n_T$
 - n_i is the number of occurences of term t_i in the collection
 - n_T is the total number of word occurences (i.e., tokens) in the collection
 - Bigram language model
 - $P(t_i | t_{i-1}) = n(t_{i-1}, t_i) / n(t_{i-1})$
 - n(t_{i-1}, t_i) is the number of occurences of bigram t_{i-1}t_i in the collection
 - n(t_{i-1}) is the number of occurrences of term t_{i-1} in the collection

Estimating probabilities – example

- We are given a toy collection consisting of three documents
 - d₁: "Frodo and Sam stabbed orcs"
 - d₂: "Sam chased the orc with the sword"
 - d₃: "Sam took the sword"
- Estimating word probabilities for the unigram model:

t_i	Frodo	Sam	orc	chased	sword	
$P(t_i)$	1/16	3/16	2/16	1/16	2/16	

Estimating the conditional probabilities for the bigram model:

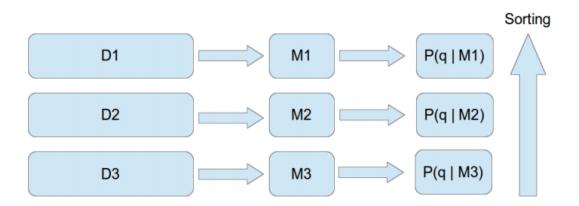
t_{i-1}, t_i	Frodo, chased	the, sword	the, orc	
$P(t_i t_{i-1})$	0	2/3	1/3	

Outline

- Recap of Lecture #5
- Language Models
 - Unigram LM
 - Bigram LM
- Query likelihood model for ranking
- Smoothing schemes

Query likelihood model for ranking

- 20
- Given a document collection D and a query q we need to estimate the probability P(q | d) for every document d in D
- In the query likelihood model, we estimate the probability P(q | d) as the probability that the language model built from d generates the query q
- Algorithm
 - Compute the language model M_i for every document d_i in D
 - Compute the probability P(q | Mi) for every language model M_i



Intuition: Language models of relevant documents should assign higher probability for the query

Query likelihood model for ranking – example

- 21
- We are given a toy collection consisting of three documents
 - d₁: "Sam chased the orc with the sword"
 - d₂: "Frodo and Sam stabbed orcs"
 - d₃: "Sam took the sword"
- We are given the query "Sam and orc and sword"
- Let's rank the documents according to unigram LM for IR (ignore stopwords)
- Step 1: Compute language models of individual documents
 - M₁: P("sam") = 0.25, P("chase") = 0.25, P("orc") = 0.25, P("sword") = 0.25
 - M₂: P("frodo") = 0.25, P("sam") = 0.25, P("stab") = 0.25, P("orc") = 0.25
 - M₃: P("sam") = 0.33, P("took") = 0.33, P("sword") = 0.33

Query likelihood model for ranking – example

- 22
- We are given a toy collection consisting of three documents
 - d₁: "Sam chased the orc with the sword"
 - d₂: "Frodo and Sam stabbed orcs"
 - d₃: "Sam took the sword"
- We are given the query "Sam and orc and sword"
- Let's rank the documents according to unigram LM for IR (ignore stopwords)
- Step 2: Let's compute the probabilities P(q | M_i)

P(q | M₁) = P("sam" | M₁) * P("orc" | M₁) * P("sword" | M₁) = 0.25 * 0.25 * 0.25

- $P(q | M_2) = P(\text{,sam}'' | M_2) * P(\text{,orc}'' | M_2) * P(\text{,sword}'' | M_2) = 0.25 * 0.25 * 0$
- $P(q | M_3) = P(\text{"sam"} | M_3) * P(\text{"orc"} | M_3) * P(\text{"sword"} | M_3) = 0.33 * 0 * 0.33$
- Q: Is there any problem with query likelihoods given LMs of d₂ and d₃?

Outline

- Recap of Lecture #5
- Language Models
 - Unigram LM
 - Bigram LM
- Query likelihood model for ranking
- Smoothing schemes

Smoothing language models

- Zero frequency problem: Models we've considered so far give probability of 0 to queries containing any term that does not occur in the document
- We can prevent this by using smoothing techniques
- Smoothing techniques
 - Change the probability distribution of terms in the language model
 - Assign some small probability to unseen words
- Three prominent smoothing schemes
 - Laplace smoothing
 - Jelinek-Mercer smoothing
 - Dirichlet smoothing

Laplace smoothing

Laplace smoothing

- 1. Adds a fixed small count (often it's 1) to all word counts
- 2. Renormalizes to get a probability distribution

$$P(t_i|M_d) = \frac{n_{i,d} + \alpha}{n_d + |V| \cdot \alpha}$$

The probability of any unseen word equals

$$P(t_{uns}|M_d) = \frac{\alpha}{n_d + |V| \cdot \alpha}$$

• Q: What might be a potential shortcoming of the Laplace smoothing?

Jelinek-Mercer smoothing

- Laplace smoothing assumes that all unseen words are equally likely
- Jelinek-Mercer smoothing (also known as interpolated smoothing)
 - 1. Additionally builds a language model M_D from the whole document collection D
 - 2. Interpolates between probabilities of the query according to the
 - Local LM language model M_d built from the particular document d
 - Global LM language model M_D built from the whole collection

$$P(t_i|M_d) = \lambda \cdot P(t_i|M_d) + (1-\lambda) \cdot P(t_i|M_D)$$

- The probability of a word unseen in the document d still gets some probability from the global language model
 - Probability of an unseen word depends on its frequency in whole collection
- Q: What if P(t_i | M_D) = 0?

Dirichlet smoothing

Dirichlet smoothing can be seen as a generalization of the Laplace smoothing

- Each word unseen in the document gets an artificial extra count
- But the extra count is not fixed, depends on the global probability of the term
 - In this respect, Dirichlet smoothing is similar to Jelinek-Mercer smoothing

$$P(t_i|M_d) = \frac{n_{i,d} + \mu \cdot P(t_i|M_D)}{n_d + \mu}$$

- Less frequent words in the document get more probability from the global component
 - The value of the constant µ determines the scale of the global probability's contribution

Language models for IR vs. VSM

- Let's compare the query likelihood model with the VSM model
- 1. Do we have a term frequency component in LM?
 - Q: do query terms that are more frequent in the document contribute more to the relevance score?
 - A: Yes! P(t_i) = n_i / n_T
- 2. Do we have a document frequency component in LM?
 - Q: does the global document frequency of the query term affect the relevance scores?
 - A: No! If we use Jelinek-Mercer or Dirichlet smoothing, we take into consideration collection frequency, but not document frequency
 - However, mixing term frequency (within document) and collection frequency has an effect similar to using IDF

Language models for IR vs. VSM

- Let's compare the query likelihood model with the VSM model
- 3. Does LM for IR account for different lengths of documents?
 - Q: Does it somehow normalize the frequencies of query terms in documents with the document length?
 - A: Yes! P(t_i) = n_i / n_T
- LM for IR vs. VSM: commonalities
 - 1. Term frequency directly in the model
 - 2. Contributions of terms are normalized to account for document length
- LM for IR vs. VSM: differences
 - 1. LM for IR is based in probability theory, VSM in vector algebra
 - 2. Collection frequency (LM) vs. Document frequency (VSM)

- Know what a language model is
- Understand differences between different language models (unigram, bigram)
- Understand how to use language modeling for information retrieval
- Are familiar with different smoothing schemes for LM for IR
- Are able to compare LM for IR with vector space model and classic probabilistic models