

## Exercise Sheet #6

### Advanced Algorithms (WS 2022/23)

#### Exercise 1 – Maximum agreement forest

For the definition of an agreement forest of two phylogenetic trees  $T$  and  $T'$ , we required that the roots of  $T$  and  $T'$  are labeled  $\rho$ . Show why this requirement is necessary for the equality  $m(T, T') = d_{\text{SPR}}(T, T')$  to always hold.

*Hint:* Show an example with different  $d_{\text{SPR}}(T, T')$  and  $m(T, T')$ .

**5 Points**

#### Exercise 2 – Connectedness of SPR-graph

Show that the SPR-graph  $G$  is connected.

**5 Points**

#### Exercise 3 – Common subtree reduction

Let  $T$  and  $T'$  be two phylogenetic trees on  $X = \{1, 2, 3, \dots, n\}$ . Give an efficient algorithm to exhaustively apply the common subtree reduction to  $T$  and  $T'$ .

**6 Points**

#### Exercise 4 – Nearest neighbor interchange

The rearrangement operation *nearest neighbor interchange* (NNI) transforms one phylogenetic tree into another one as illustrated in Figure 1. Note that NNI is a restriction of SPR. Determine the size of the neighborhood of a phylogenetic tree  $T$  on  $n$  leaves under NNI, that is, the number of trees that can be reached from  $T$  by applying one NNI operation.

**4 Points**

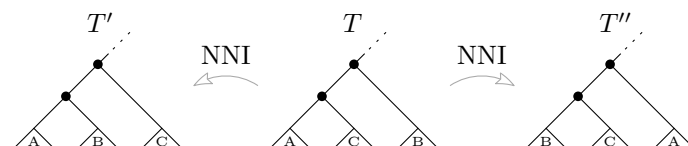


FIGURE 1: How an NNI operation can transform a phylogenetic tree  $T$  into a phylogenetic tree  $T'$  or  $T''$ . The triangles labeled A, B, and C represent different pendant subtrees.

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Please hand in your solutions on Wuecampus until the beginning of the next lecture, that is 14:15 on Wednesday, November 30.